# Real-time Tissue Tracking with B-Mode Ultrasound Using Speckle and Visual Servoing 

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#### Abstract

We present a method for real-time tracking of moving soft tissue with B-mode ultrasound (US). The method makes use of the speckle information contained in the US images to estimate the in-plane and out-of-plane motion of a fixed target relative to the ultrasound scan plane. The motion information is then used as closed-loop feedback to a robot which corrects for the target motion. The concept is demonstrated for translation motions in an experimental setup consisting of an ultrasound speckle phantom, a robot for simulating tissue motion, and a robot that performs motion stabilization from US images. This concept shows promise for US-guided procedures that require real-time motion tracking and compensation.


## 1 Introduction

Quantitative ultrasound guidance (US) has great potential for aiding a wide range of diagnostic and minimally invasive surgical applications. However, one of the barriers to wider application is the challenge of locating and maintaining targets of interest within the US scan-plane, particularly when the underlying tissue is in motion. This problem can be alleviated, to some degree, through the use of recently developed 3D ultrasound systems. However, a more practical solution is to create a means of stabilizing a traditional B-mode ultrasound imager relative to a target. This capability can be exploited in many applications, for example to automatically move the US probe to maintain an appropriate view of moving soft tissues during US scanning or to synchronize the insertion of a needle into a moving target during biopsy or local therapy.

In this paper, we present a system that is capable of fully automatic, realtime tracking and motion compensation of a moving soft tissue target using a sequence of B-mode ultrasound images. Contrary to prior work in this area, which has relied on segmenting structures of interest [1,2], we make direct use of the speckle information contained in the US images. While US speckle is usually considered to be noise from an imaging point of view, it in fact results from the coherent reflection of microscopic structures contained in soft tissue. As such,

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Fig. 1. (left) Experimental decorrelation curves obtained by measuring the correlation value between 25 patches of B-scan $\mathbf{I}_{\mathbf{1}}$ and their corresponding patches in B-scan $\mathbf{I}_{\mathbf{2}}$ along the elevation distance $d$ (right)
it is spatially coherent. Furthermore, an US beam is several mm wide. As a result, there is substantial overlap between US scan planes with small lateral displacements and, therefore, substantial correlation of the speckle information between successive images. Speckle correlation occurs for both in-plane and out-of-plane motion, thereby making it possible to track both out-of plane and inplane motion, and raising the possibility of calculating full 6 -DOF relative pose of speckle patches.

Initially, speckle information has been used to estimate multi-dimensional flow in 2D ultrasound image ([3]). Recently several authors ([4, 5]) have published speckle decorrelation techniques to allow freehand 3D US scanning without a position sensor on the US probe. Their techniques depend on experimentally calibrating speckle decorrelation curves from real soft tissues and/or speckle simulating phantoms. These curves (Fig. 1) are obtained by capturing B-mode images at known distances $d$ along the elevation direction (i.e. orthogonal to the image plane) and measuring the normalized correlation coefficients for a finite number of rectangular patches fixed in the images. The imaging procedure then entails capturing an US stream by moving the probe in a given direction. The relative in-plane and out-of-plane position between each image is then estimated, off-line, from the estimated elevation distances from at least 3 non-collinear patches in the image plane. These distances are computed from the calibrated decorrelation curves using the measured inter-patch correlation value for each image patch.

In our experimental scenario, we also perform an offline calibration procedure to relate speckle decorrelation to elevation motion. However, we subsequently servo the US probe to track a user-selected B-scan target in a fully automatic, online manner. The 6 -DOF motion of the target B-scan is extracted by an estimation method using the speckle information and an image region tracking algorithm based on grey level intensity. A visual servoing scheme is then used
to control the probe displacement. Section 2 presents the methods used to extract 6 -DOF rigid motion of the target B-scan image. The visual servoing control laws are developed in section 3 and section 4 presents first results obtained from ex-vivo experiments where only translation motions are considered.

## 2 Motion extraction

The overall tracking problem is to minimize the relative position between the current B-scan (denoted by a Cartesian frame $\{c\}$ ) and a target B-scan (denoted by a Cartesian frame $\{i\}$ ). The full 6 DOF target plane position can be decomposed by two successive homogeneous transformations: ${ }^{c} \mathbf{H}_{i}={ }^{c} \mathbf{H}_{p}{ }^{p} \mathbf{H}_{i}$ where ${ }^{c} \mathbf{H}_{p}$ and ${ }^{p} \mathbf{H}_{i}$ describing the in-plane and out-of-plane displacement of the target, respectively. Note that $\{p\}$ corresponds to an intermediate "virtual" plane. The in-plane displacement corresponds to the translations $x$ and $y$ along the $X$ and $Y$ axes of the current image plane and the angular rotation $\gamma$ around the $Z$ axis (orthogonal to the image), such that:

$$
{ }^{c} \mathbf{H}_{p}=\left(\begin{array}{cccc}
\cos (\gamma) & -\sin (\gamma) & 0 & x  \tag{1}\\
\sin (\gamma) & \cos (\gamma) & 0 & y \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right)
$$

We use a classical template tracking technique [6] to extract the in-plane motion parameters $x, y, \gamma$. This information is then used to relate the image coordinates of patches in the two images for the purposes of estimating out-of-plane motion using speckle decorrelation.

To extract the out-of-plane motion, we use the Gaussian model introduced in [4]. From experimental observations (Fig. 1), we found that the elevation distance between a patch in the target plane and the corresponding patch in the current image can be estimated by $\hat{d}=\sqrt{-2 \hat{\sigma}^{2} \ln (\rho)}$, where $\hat{\sigma}=0.72 \mathrm{~mm}$ is the mean resolution cell width (identified from experimental decorrelation curves).

To compute the full out-of-plane motion, we compute the elevation distance of a grid of patches ( 25 in our current system) , and fit a plane to this data. However, the Gaussian model does not detect the sign of the elevation distance for a given patch. Thus, we employ the following algorithm to estimate the out-ofplane position of the target plane with respect to the virtual plane $\{p\}$. We first set a random sign on each inter-patch distance and estimate (with a least-square algorithm) an initial position of the target plane using these signs. We then use the iterative algorithm we presented in [7] to determine the correct signed distances and the associated plane. This algorithm, which minimizes the leastsquare error of the estimated target plane, converges to two stable solutions that are symmetrical around plane $\{p\}$. The two solutions correspond to the positive and negative elevation distances $z$, respectively. Note that from one solution we can easily determine the second. By formulating the out-of-plane relative position as a combination of a translation $z$ along the $Z$ axis of plane $\{p\}$ and
two successive rotations $\alpha, \beta$ around the $Y$ and $X$ axes of $\{p\}$, we obtain the following homogeneous transformation matrix for out-of-plane motion:

$$
{ }^{p} \mathbf{H}_{i}=\left(\begin{array}{cccc}
\cos (\alpha) & \cos (\alpha) \sin (\theta) & \sin (\alpha) \cos (\theta) & 0  \tag{2}\\
0 & \cos (\theta) & -\sin (\theta) & 0 \\
-\sin (\alpha) & \cos (\alpha) \sin (\theta) & \cos (\alpha) \cos (\theta) & z \\
0 & 0 & 0 & 1
\end{array}\right)
$$

The two symmetrical solutions for the 6 DOF motion are then given by the estimates:

$$
\begin{equation*}
{ }^{c} \widehat{\mathbf{H}}_{i}(+)={ }^{c} \widehat{\mathbf{H}}_{p}{ }^{p} \widehat{\mathbf{H}}_{i}(+) \quad \text { and } \quad{ }^{c} \widehat{\mathbf{H}}_{i}(-)={ }^{c} \widehat{\mathbf{H}}_{p}{ }^{p} \widehat{\mathbf{H}}_{i}(-) \tag{3}
\end{equation*}
$$

where $(+)$ indicates the solution obtained for $\hat{z}>0$, with $\hat{\alpha}=\operatorname{atan}(\hat{a} / \hat{c})$, $\hat{\theta}=-\operatorname{asin}(\hat{b})$ and (-) indicates the solution corresponding to $\hat{z}<0$ with $\hat{\alpha}=\operatorname{atan}(-\hat{a} / \hat{c}), \hat{\theta}=-\operatorname{asin}(-\hat{b})$. Here $(\hat{a}, \hat{b}, \hat{c})$ is the normal vector of the estimated target plane that is obtained for the solution $\hat{z}>0$. The subscript ${ }^{\wedge}$ denotes values provided by the template tracking and plane estimation methods. It will be purposely dropped in the next of the paper for clarity of presentation.

This method works only locally about the target region due to the rapid rate of speckle decorrelation with out-of-plane motion. Therefore, in order to increase the range of convergence, we augment the basic algorithm with a FIFO buffer of intermediate planes $\{i\}$ between the target $\{t\}$ and current plane $\{c\}$. These planes, which are acquired online as the probe moves, are chosen to be close enough to be well "speckle correlated" and thus provide a "path" of ultrasound images that can be traced back to the target.

The complete algorithm summarizing our method for extracting target plane position is described in Fig. 2 (for positive elevation distances) and Fig. 3 (for negative elevation distances.) At initialization, the target plane is captured in the initial B-scan image and stored in a FIFO buffer (plane) starting with index $i=0$. The current image is also stored as the target image (imagereference $=$ currentplane). A small negative elevation displacement is then applied to the probe in order to obtain an initial positive elevation distance $z[0] \geq s>0$ of plane $[0]$ with respect to the current B-scan plane. Here $s$ is a small threshold distance fixed to guarantee speckle correlation between US images. The algorithm goes to the case of positive elevation distance. The array index is then incremented and an intermediate plane is stored (plane $[i]=$ currentplane) with the homogeneous matrix ${ }^{i} \mathbf{H}_{i-1}={ }^{c} \mathbf{H}_{i-1}(+)$ describing the position of plane $[i-1]$ with respect to plane $[i]$ and given by (3). Each time an intermediate plane is added, the target image used by the in-plane motion tracker is also updated (imagereference $=$ currentplane). After initialization, the configuration of planes corresponds to case 1 in Fig. 2, where the target plane position is ${ }^{c} \mathbf{H}_{t}={ }^{c} \mathbf{H}_{i}(+) \prod_{i}^{1}{ }^{k} \mathbf{H}_{k-1}$. Now, we suppose that the target plane moves for some reason. By computing (3) for ${ }^{c} \mathbf{H}_{i}$ and ${ }^{c} \mathbf{H}_{i-1}$, we can: 1) determine the consistent pair of solutions that express the current plane relative to plane[i] and plane $[i-1], 2$ ) determine which of cases 1,2 or 3 is valid and 3 ) compute the target elevation position ${ }^{c} \mathbf{H}_{t}$ accordingly. As shown, the three cases are: 1)


Fig. 2. (top) possible planes configurations and (bottom) process used to manage the intermediates planes when the target elevation distance is positive
if the current plane moves a distance $s$ beyond the top of the FIFO array, then a new intermediate plane is added or 2 ) if the current plane is between the top two planes of the FIFO array, then no change occurs, or 3) if the elevation distance decreases, then the last intermediate plane is removed from the FIFO array. In the latter case, a special situation arises when there are only two planes $(i=1)$ in the array. In this case, if the absolute value of the target elevation distance reaches the threshold $s$, then the algorithm switches to the second mode described in Fig. 3 which is the symmetric logic for negative elevations. For this mode, the possible configurations of planes are illustrated by cases 4 to 6 in Fig. 3. The algorithm switches back to the first mode when the target plane elevation position becomes positive again.

## 3 Visual servoing

Now, as the position of the B-scan target with respect to the current plane has been estimated, we move the robot (holding the probe) in order to follow the target plane. In our approach, a 3D visual servoing control scheme is used to minimize the relative position between the current and target planes. The error vector is the 6 dimensional pose vector $\mathbf{x}=\left({ }^{t} \mathbf{P}_{\mathbf{c}}^{\mathbf{T}}, \theta \mathbf{u}^{\mathbf{T}}\right)^{\mathbf{T}}$ describing the


Fig. 3. (top) possible planes configurations and (bottom) process used to manage the intermediates planes when the target elevation distance is negative
position of the current plane frame $\{c\}$ with respect to the target plane frame $\{t\}$. Here ${ }^{t} \mathbf{P}_{\mathbf{c}}$ is the translation vector obtained directly from the 4 th column of ${ }^{t} \mathbf{H}_{c}={ }^{c} \mathbf{H}_{t}^{-1}$, and $\theta \mathbf{u}$ is the angle-axis representation of the rotation ${ }^{t} \mathbf{R}_{c}$ [8].

The variation of $\mathbf{x}$ is related to the velocity screw $\mathbf{v}=\left(v_{x}, v_{y}, v_{z}, \omega_{x}, \omega_{y}, \omega_{z}\right)^{T}$ of the ultrasound probe by $\dot{\mathbf{x}}=\mathbf{L}_{s} \mathbf{v}$. In visual servoing, $\mathbf{L}_{s}$ is called the interaction matrix and is given in this case by (cf. [9]):

$$
\mathbf{L}_{s}=\left(\begin{array}{cc}
{ }^{t} \mathbf{R}_{c} & \mathbf{0}_{3}  \tag{4}\\
\mathbf{0}_{3} & \mathbf{I}_{3}-\frac{\theta}{2}[\mathbf{u}]_{\times}+\left(1-\frac{\operatorname{sinc} \theta}{\operatorname{sinc}^{2} \frac{\theta}{2}}\right)[\mathbf{u}]_{\times}
\end{array}\right)
$$

where $\mathbf{I}_{3}$ is the $3 \times 3$ identity matrix and $[\mathbf{u}]_{\times}$is the skew matrix of the vector preproduct linked with $\mathbf{u}$. The visual servoing task (cf. [9]) can then be expressed as a regulation to zero of the pose $\mathbf{x}$ and is performed by applying the following control law: $\mathbf{v}=-\lambda \mathbf{L}_{s}^{-1} \mathbf{x}$ where $\lambda$ is the proportional coefficient involved for a exponential convergence.

## 4 Experiments and Results

We have tested the motion stabilization method on 2-DOF motions combining a translation along the image X axis (in-plane translation) and elevation Z axis


Fig. 4. (top) experimental setup - (bottom-left) evolution of the robots positions -(bottom-right) tracking error
(out-of-plane translation). The experimental, setup, shown in Fig. 4, consists of two X-Z Cartesian robots fixed and aligned on an optical table. The first robot provides a ground truth displacement for an US speckle phantom. The second robot holds a transrectal 6.5 Mhz US transducter and is controlled as described above to track a target plane. The US image is $440 \times 320$ pixels with resolution of $0.125 \mathrm{~mm} /$ pixel. A laptop computer (Pentium IV 2 Ghz ) captures the US stream at 10 fps , extracts the target plane position by using a grid of 25 patches and computes the velocity control vector applied to the probe holding robot. The plots in Fig. 4 show the evolution of the robots positions and the tracking error when sinusoidal motions (magnitude of 30 mm on each axis) were applied to the phantom. The dynamic tracking error was below 3 mm for in-plane translation and 3.5 mm for the elevation translation. This error is attributed the dynamics of the target motion, time delays in the control scheme, and the dynamics of the probe holding robot. These errors could be reduced if a prediction of its variation was introduced into the control law by some method
such as Kalman filter or generalized predictive controller [10]. Adopting recent methods [11] for more accurate and efficient identification of fully developed speckle patches should also improve on tracking performance and may allow estimation of relative motion between different soft tissue elements. In order to determine the static accuracy of the tracking robotic task, we applied a set of 140 random positions to the phantom by using ramp trajectories while tracking the target plane by the robotized probe. When the probe stabilized at a position, the phantom was held motionless for 2 seconds and the locations of the two robots were recorded. We recorded a static error of $0.0219 \pm 0.05 \mathrm{~mm}$ (mean $\pm$ standard deviation) for the in-plane tracking and $0.0233 \pm 0.05 \mathrm{~mm}$ for the out-of-plane tracking, which is close to the positioning accuracy of the robots ( $\pm 0.05 \mathrm{~mm}$ ).

In conclusion, results obtained from 2-DOF in-plane and out-of-plane motions demonstrated the potential of our approach. We are presently adding rotational stages to the robots to experimentally validate full 6 -DOF motion tracking and visual servoing capabilities of the current algorithm described in this paper.

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